

## EMPIRICAL AND MOLECULAR FORMULA

**Percent Composition:** law of constant composition states that any sample of a pure compound always consists of the same elements combined in the same proportions by mass

$$\% \text{ comp} = \frac{\text{mass of element part} \times 100}{\text{mass of compound}}$$

**EXAMPLE:**

Here is  $\text{CH}_3\text{COOH}$ .

First, figure out the molar mass from the formula. It is 60.05 g/mol.

Second, figure out the grams each atom contributes by multiplying the atomic weight by the subscript.

$$\text{Carbon} = 2 \times 12.011 \text{ g} = 24.022 \text{ g}$$

$$\text{Hydrogen} = 4 \times 1.008 = 4.032 \text{ g}$$

$$\text{Oxygen} = 2 \times 16.00 = 32.00 \text{ g}$$

Third, divide the answer for each atom by the molar mass and multiply by 100 to get a percentage.

$$\text{Carbon's percentage: } (24.022 \text{ g} / 60.05 \text{ g}) \times 100 = 40.00 \%$$

$$\text{Hydrogen's percentage: } (4.032 \text{ g} / 60.05 \text{ g}) \times 100 = 6.71 \%$$

$$\text{Oxygen's percentage: } (32.00 \text{ g} / 60.05 \text{ g}) = 53.29 \%$$

**Empirical and Molecular Formulas:** assume 100 g sample if given %'s

**Empirical** formula: subscripts represent the smallest ratio of atoms in a formula unit:

- 1) convert all grams (=%) to moles
- 2) divide by smallest # of moles
- 3) create whole number ratio of subscripts (multiply through by integer if needed)

**EXAMPLE:**

In an unknown molecule, there is 4.15 g carbon and 1.38 g hydrogen. Determine the empirical formula for the substance.

Step 1. Divide mass of each substance by atomic mass to determine number of moles of each substance

$$4.15 \text{ g C} / 12.0 \text{ g C} = .346 \text{ mol C}$$

$$1.38 \text{ g H} / 1 \text{ g H} = 1.38 \text{ mol H}$$

Step 2. Divide number of moles of each substance by smallest number of moles to determine what the ratio of carbon is to hydrogen

$$.346 \text{ mol C} / .346 \text{ mol C} = 1$$

$$1.38 \text{ mol H} / .346 \text{ mol C} = 4$$

This indicates that for every 1 carbon atom there are 4 hydrogen atoms.

The empirical formula would be  $\text{CH}_4$ .

**EXAMPLE:**

Phenol, a general disinfectant, is 76.57% C, 6.43% H, and 17.00% O. Determine its empirical formula.

Step 1. A 100.00g sample of phenol contains 76.57g C, 6.43g H, 17.00g O.

Step 2. Convert the masses of C, H, and O to numbers of moles.

$$\begin{array}{l}
 76.57\text{g C} \times \frac{1 \text{ mol C}}{12.011 \text{ g C}} = 6.375 \text{ mol C} \\
 6.43\text{g H} \times \frac{1 \text{ mol H}}{1.008 \text{ g H}} = 6.38 \text{ mol H} \\
 17.00\text{g O} \times \frac{1 \text{ mol O}}{15.999 \text{ g O}} = 1.063 \text{ mol O}
 \end{array}$$

Step 3. Divide each of the quantities above by the smallest, and use the result as subscripts in a tentative formula.

$$\begin{array}{l}
 \text{C} = 6.375/1.063 = 5.997 \\
 \text{H} = 6.38/1.063 = 6.00 \\
 \text{O} = 1.063/1.063 = 1.000 \\
 \text{C}_6\text{H}_6\text{O}
 \end{array}$$

Since all the subscripts are integers, there is no need to multiply each subscript by a common factor to convert them all to integers.

The empirical formula of phenol is  $\text{C}_6\text{H}_6\text{O}$ .

**Molecular** formula represents the actual # of atoms in a molecule:

- 1) Need to be given molar mass of actual compound.
- 2) Calculate molar mass of your empirical formula
- 3) Molar mass of compound  $\div$  molar mass of empirical formula = multiple of number of atoms in molecular formula
- 4) Apply multiple to empirical ratio

The empirical formula of hydroquinone, a chemical used in photography, is  $\text{C}_3\text{H}_3\text{O}$ , and its molecular weight is 110 g/mol.

What is its molecular formula?

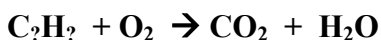
The formula weight based on the empirical formula is 55g/mol. If all the subscripts are multiplied by two

( $110/55.0 = 2$ ), the molar mass of the empirical formula becomes equal to the molecular weight or molar mass of the compound

$$2(55.0\text{g/mol}) = 110\text{g/mol.}$$

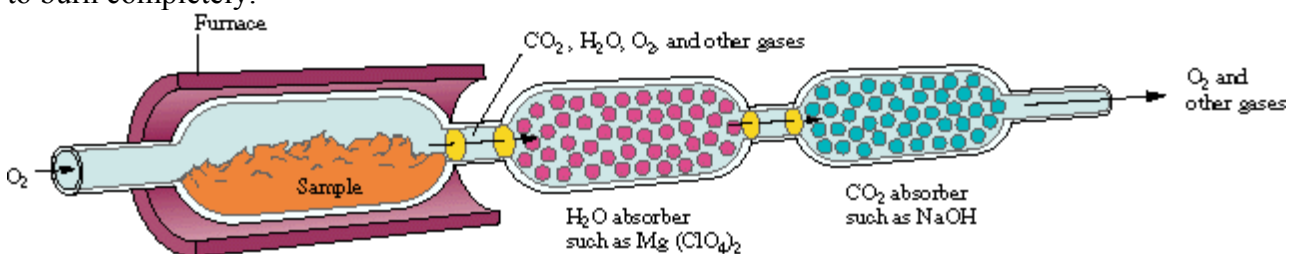
The molecular formula is  $2(\text{C}_3\text{H}_3\text{O})$  or  $\text{C}_6\text{H}_6\text{O}_2$

## ANALYSIS BY COMBUSTION



- All carbons go to carbon dioxide
  - All hydrogens go to water
- ✓ To find formulas we need grams of carbon and grams of hydrogen in original hydrocarbon.
  - ✓ Grams of Carbon  $\rightarrow$  the molar mass of  $\text{CO}_2$  provides a conversion factor between g C and g  $\text{CO}_2$  (12.01 g C = 44.01 g  $\text{CO}_2$ )
  - ✓ Grams of Hydrogen  $\rightarrow$  the molar mass of  $\text{H}_2\text{O}$  provides a conversion factor between g of H and g of  $\text{H}_2\text{O}$  (2.02 g H = 18.02 g  $\text{H}_2\text{O}$ )
  - ✓ If compound also contains oxygen,  
g of oxygen = sample mass - [g of C + g of H]
  - ✓ Grams are converted to moles

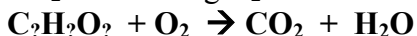
In practice, a combustible sample is placed in an oven under an oxygen stream and heated to burn completely.



The  $\text{H}_2\text{O}$  formed gas stream is trapped in a desiccant such as  $\text{Mg}(\text{ClO}_4)_2$ , the  $\text{CO}_2$  is absorbed in a base (like  $\text{NaOH}$ ), and the excess  $\text{O}_2$  just vents off. Weighing the traps before and after the combustion gives one the weight of the evolved  $\text{CO}_2$  and  $\text{H}_2\text{O}$ .

### EXAMPLE:

Imagine that a 5.0000 g sample of some unknown containing the elements C, H and O (actually acetic acid) is subjected to such a combustion analysis. The traps yield 7.3285 g  $\text{CO}_2$  and 3.000 g  $\text{H}_2\text{O}$ .



**Find grams of C and H** to find oxygen subtract grams of H and C from mass of sample:

But  $\text{CO}_2$  isn't C, and  $\text{H}_2\text{O}$  isn't H.

We need the molar mass of CO<sub>2</sub> and water

$$\begin{aligned} \text{Molar masses CO}_2 &= (\text{AW C}) + 2 \times (\text{AW O}) \\ &= 12.011 \text{ g/mol} + 2(15.999 \text{ g/mol}) = 44.009 \text{ g CO}_2 / \text{mol CO}_2 \end{aligned}$$

$$7.3285 \text{ g CO}_2 \times \frac{12 \text{ g C}}{44.009 \text{ g CO}_2} = 1.998 \text{ g C or } 2.00 \text{ g C}$$

$$\begin{aligned} \text{MW H}_2\text{O} &= (\text{AW O}) + 2 \times (\text{AW H}) \\ &= 15.999 \text{ g/mol} + 2(1.008 \text{ g/mol}) = 18.015 \text{ g H}_2\text{O} / 1 \text{ mol H}_2\text{O} \end{aligned}$$

$$3.00 \text{ g H}_2\text{O} \times \frac{2 \text{ g H}}{18.015 \text{ g H}_2\text{O}} = 0.3357 \text{ g H}$$

**Grams O** = So a total of 2.000 g C + 0.3357 g H = 2.336 g of the unknown is C and H.  
The rest, 5.0000 g sample - 2.336 g C and H = **2.664 g O**

### Convert g to MOLES

$$\text{C} = \frac{2.00 \text{ g}}{12 \text{ g/mol}} = 0.1666666 \text{ mole of C}$$

$$\text{H} = \frac{0.3357 \text{ g}}{1 \text{ g/mol}} = 0.3357 \text{ mole H}$$

$$\text{O} = \frac{2.6664 \text{ g}}{16 \text{ g/mol}} = 0.16665 \text{ mole O}$$

### Determine molar ratio:

$$\text{C} = 0.166666 \text{ mole} / 0.16665 \text{ mole} = 1$$

$$\text{H} = 0.3357 / 0.16666 \text{ mole} = 2$$

$$\text{O} = 0.16665 \text{ mole} / 0.16665 \text{ mole} = 1$$



### Exercises

1. The molecular formula of the antifreeze ethylene glycol is C<sub>2</sub>H<sub>6</sub>O<sub>2</sub>. What is the empirical formula?
2. A well-known reagent in analytical chemistry, dimethylglyoxime, has the empirical formula C<sub>2</sub>H<sub>4</sub>NO. If its molar mass is 116.1 g/mol, what is the molecular formula of the compound?
3. Nitrogen and oxygen form an extensive series of oxides with the general formula N<sub>x</sub>O<sub>y</sub>. One of them is a blue solid that comes apart, reversibly, in the gas phase. It contains 36.84% N. What is the empirical formula of this oxide?

4. A sample of indium chloride weighing 0.5000 g is found to contain 0.2404 g of chlorine. What is the empirical formula of the indium compound?
5. A combustion device was used to determine the empirical formula of a compound containing only carbon, hydrogen, and oxygen. If the data determined from a .6349 g sample of the unknown is that 1.603 g of  $\text{CO}_2$  and .2810 g of  $\text{H}_2\text{O}$  were produced, determine the empirical formula of the compound.
6. The analysis of a rocket fuel showed that it contained 87.4% nitrogen and 12.6% hydrogen by weight. Mass spectral analysis showed the fuel to have a molar mass of 32.05g. What are the empirical and molecular formulas of the fuel?

Answers:

1.  $\text{CH}_3\text{O}$
2. Molar mass of empirical formula is 58.06 g/mol. Thus molecular formula is  $\text{C}_4\text{H}_8\text{N}_2\text{O}_2$ .
3. The empirical formula is thus  $\text{N}_2\text{O}_3$ . (The name is dinitrogen trioxide.)
4.  $\text{InCl}_3$ .
5.  $\text{C}_7\text{H}_6\text{O}_2$
6. empirical formula:  $\text{NH}_2$   
molecular formula:  $\text{N}_2\text{H}_4$   
(the compound is called hydrazine)